

Distance Bounding Protocols: Computational vs. Symbolic Models

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(joint work with S. Mauw, Z. Smith and R. Trujillo)

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Luxembourg National
Research Fund



Outline

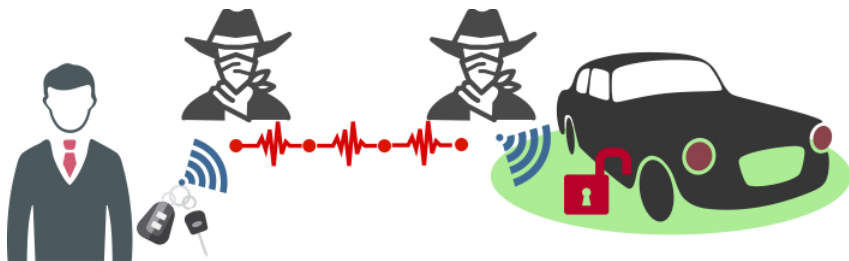
- 1 Introduction
- 2 Probabilistic model based on automata
- 3 Symbolic model with time and location
- 4 Symbolic model based on causality
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This talk's content

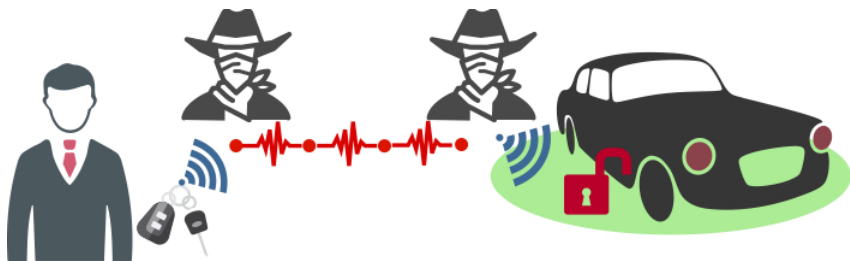
- S. Mauw, J. Toro-Pozo, R. Trujillo-Rasua, “A Class of Precomputation-Based Distance-Bounding Protocols”, in *EuroS&P'16*, 2016, pp. 97–111.
- S. Mauw, J. Toro-Pozo, R. Trujillo-Rasua, “Optimality Results on the Security of Lookup-Based Protocols”, in *RFIDSec'16*, 2016, pp. 137–150.
- S. Mauw, Z. Smith, J. Toro-Pozo, R. Trujillo-Rasua, “Distance Bounding Protocols: Verification without Time and Location”, in *S&P'18*, 2018.

Problem: Relay attack



Source: securepositioning.com

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Definition

A *relay attack* is a man-in-the-middle attack in which an attacker relays verbatim a message from the sender to a valid receiver.

Solution: Distance-bounding protocols

Definition

A *distance-bounding protocol* is an authentication protocol that checks that the distance between verifier and prover is below a given threshold.

Solution: Distance-bounding protocols

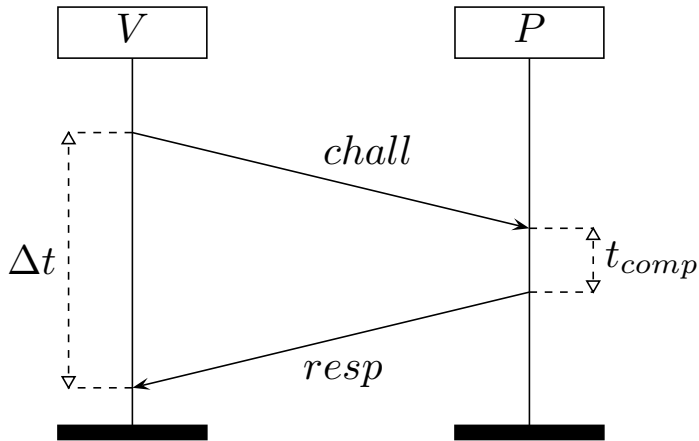
Definition

A *distance-bounding protocol* is an authentication protocol that checks that the distance between verifier and prover is below a given threshold.

How to measure (or bound) distance?

- Verifier sends a challenge.
- Prover provides corresponding response.
- Verifier measures the round-trip-time.

A challenge/response round



$$\text{dist}(V, P) = \frac{1}{2} \cdot c \cdot (\Delta t - t_{comp}) \leq \frac{1}{2} \cdot c \cdot \Delta t$$

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Lookup Protocols: Motivation

- To obtain an accurate upper-bound on the distance, the computational time on the prover's side must be as short as possible.
- Solution: Pre-computing the possible responses and store them in a constant-time-access structure, such as a lookup-table.
- Protocols with a final crypto-verification phase could be outperformed by a precomputation-based protocol with more rounds, with no increase of the computational cost: $\forall n, \exists m: \left(\frac{1}{2}\right)^n > \left(\frac{3}{4}\right)^m$.
- Partial information can be given if the protocol gets interrupted before finishing.

Lookup protocols are DB protocols such that:

- 1 In the fast phase, the responses to the challenges are the result of lookup operations from a table.

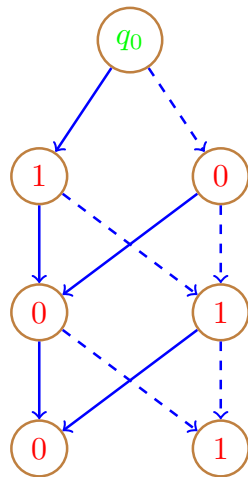
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- 1 In the fast phase, the responses to the challenges are the result of lookup operations from a table.
- 2 either do **NOT** have a final verification phase at all or
- 3 having replied correctly and on time to all challenges is **SUFFICIENT** to pass the protocol (do not have any crypto-based verification mechanism such as opening commits, keyed hash functions, signatures...).

Protocol Representation: State-Labeled DFA



$$A = (\Sigma, \Gamma, Q, q_0, \delta, \ell)$$

Σ is the set of input symbols

Γ is the set of output symbols

Q is the set of states

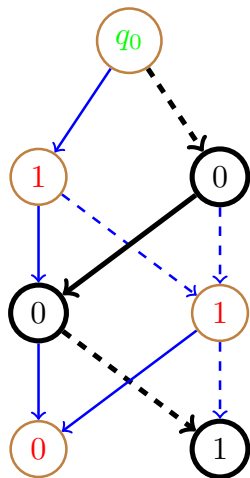
$q_0 \in Q$ is the initial state

$\delta: Q \times \Sigma \rightarrow Q$ is the transition function

$\ell: Q \rightarrow \Gamma$ is the state labeling function

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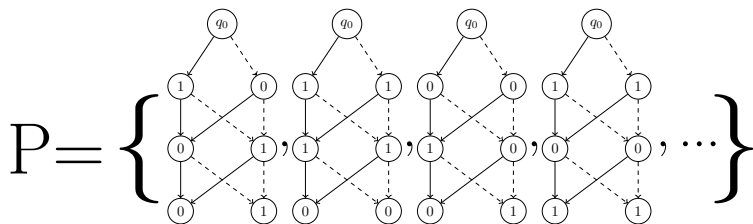
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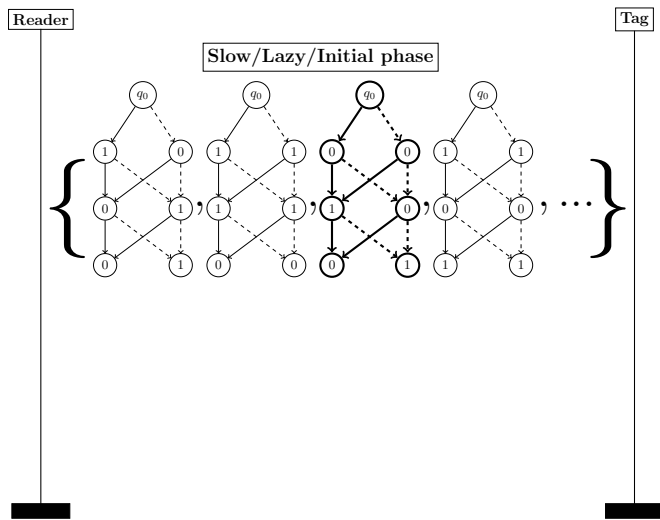
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$$\Omega_A(101) = 001$$

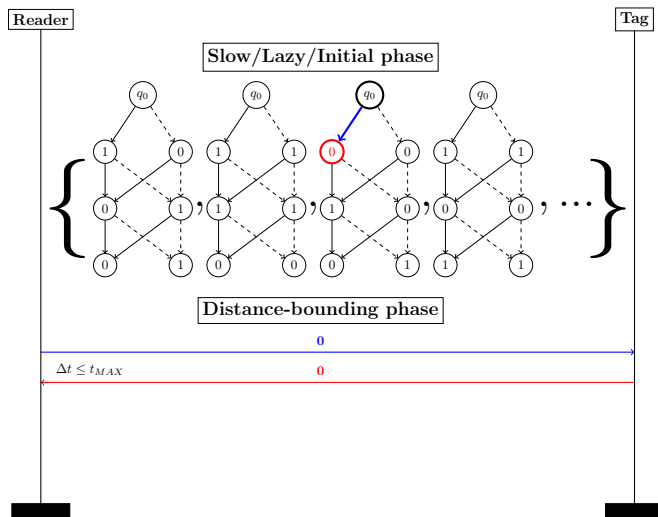
Protocol Representation



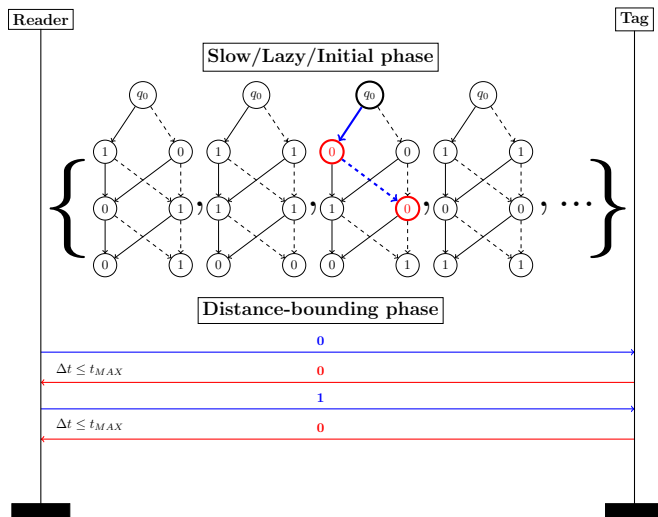
Protocol Execution



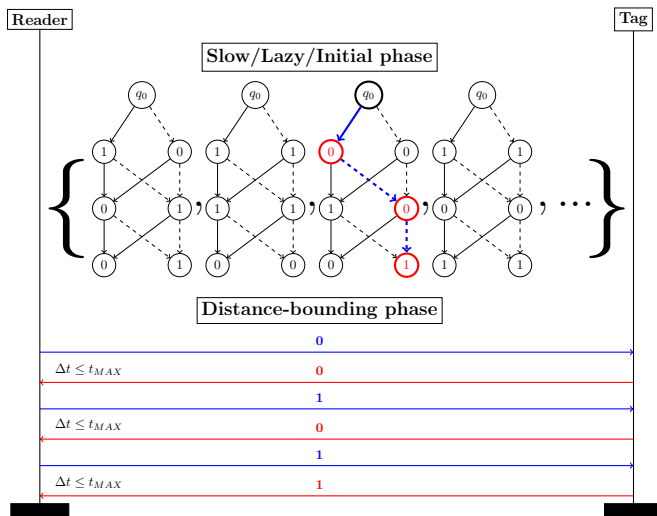
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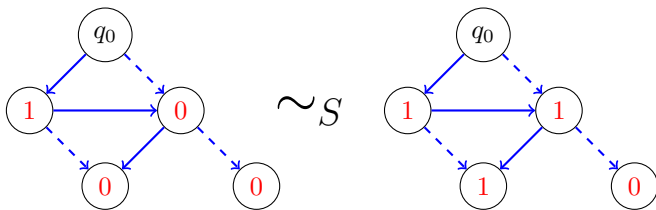
Protocol Execution



Automata Equivalence Relations

- State-label-insensitive relation (\sim_S)

$$(\Sigma, \Gamma, Q, q_0, \delta, \ell) \sim_S (\Sigma, \Gamma, Q, q_0, \delta, \ell')$$

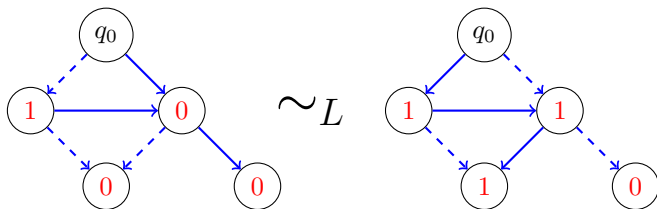


Automata Equivalence Relations

- Label-insensitive relation (\sim_L)

$$(\Sigma, \Gamma, Q, q_0, \delta, \ell) \sim_L (\Sigma, \Gamma, Q, q_0, \delta', \ell')$$

such that $\forall q \in Q : \{\delta(q, c) \mid c \in \Sigma\} = \{\delta'(q, c) \mid c \in \Sigma\}$.



Consistency and Closeness

- A protocol P is **consistent w.r.t \sim_R** iff

$$A, A' \in P: A \sim_R A'$$

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- The **closure** of P w.r.t \sim_R , denoted by P^R , is the minimal superset of P that is closed under \sim_R .

Some formulas

Given a layered automaton A :

$$mafia\left(\{A\}^S\right) = \frac{1}{|\Sigma|^n \cdot |\Gamma|^n} \max_{x \in \Sigma^n} \left\{ \sum_{y \in \Sigma^n} |\Gamma|^{collisions_A(x,y)} \right\}$$

$$mafia\left(\{A\}^L\right) = \frac{1}{|\Sigma|^{2n} \cdot |\Gamma|^n} \sum_{x,y \in \Sigma^n} |\Gamma|^{collisions_A(x,y)}$$

Some formulas

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$$\mathit{mafia}\left(\{A\}^L\right) = \frac{1}{|\Sigma|^{2n} \cdot |\Gamma|^n} \sum_{x,y \in \Sigma^n} |\Gamma|^{\mathit{collisions}_A(x,y)}$$

Trivially, $\mathit{mafia}\left(\{A\}^S\right) \geq \mathit{mafia}\left(\{A\}^L\right)$

because $\max \{u_i\} \geq \frac{1}{N} (u_1 + \dots + u_N)$

Theorem

For any layered lookup protocol P the following holds:

$$\begin{aligned} \text{mafia}(P) &\geq \text{mafia}(P^S) \geq \\ &\text{mafia}(\{A\}^L) \geq \text{mafia}(\text{Tree}), \end{aligned}$$

for some $A \in P$.

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for some $A \in P$.

- We have formalized relevant structural properties of lookup protocols that have been used in a rather intuitive way.
- We provided simple formulas for computing mafia success probability for **all but one** lookup protocols.
- We have addressed (partially) the security-memory trade-off problem in layered protocols.

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The basis of our work

Model based on time and location

- P. Schaller, B. Schmidt, D. A. Basin, and S. Capkun, “Modeling and verifying physical properties of security protocols for wireless networks,” in *CSF’09*, 2009, pp. 109–123.
- D. A. Basin, S. Capkun, P. Schaller, and B. Schmidt, “Let’s get physical: Models and methods for real-world security protocols,” in *TPHOLs’09*, 2009, pp. 1–22.
- C. J. F. Cremers, K. B. Rasmussen, B. Schmidt, and S. Capkun, “Distance hijacking attacks on distance bounding protocols,” in *S&P’12*, 2012, pp. 113–127.

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- **Specification:** a set of rules defining the actions of *honest* agents.
- And some other stuff such as **message deduction**.

- **Trace:** a sequence $(t_1, e_1) \cdots (t_n, e_n)$ with $t_i \in \mathbb{R}, e_i \in Ev$.

$$\alpha = (1.3, send_{Alice}(m)) \cdot (3, recv_{Bob}(m)) \cdot (5, send_{Bob}(h(m)))$$

- **Trace:** a sequence $(t_1, e_1) \cdots (t_n, e_n)$ with $t_i \in \mathbb{R}, e_i \in Ev$.

$$\alpha = (1.3, send_{Alice}(m)) \cdot (3, recv_{Bob}(m)) \cdot (5, send_{Bob}(h(m)))$$

$$dist(Alice, Bob) \leq c \cdot (3 - 1.3)$$

- **Specification:** a set of rules defining the actions of *honest* agents.

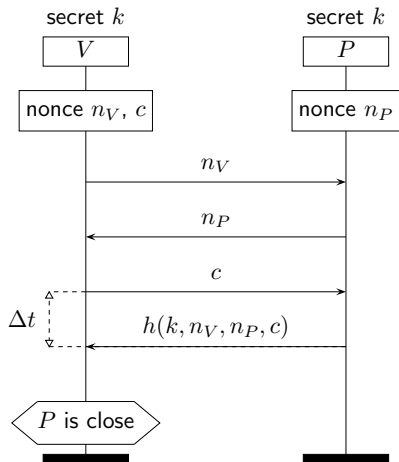
$\mathcal{P} = \{R_1 \dots, R_n\}$ where the R_i 's have the form:

$$\frac{t \geq \max t(\alpha) \quad A \in \text{Honest} \quad \text{cond}_1 \quad \dots \quad \text{cond}_n}{(\alpha, (t, e)) \in R_i}$$

In words: if conditions cond_j are met, then the agent A can execute the event e at time t .

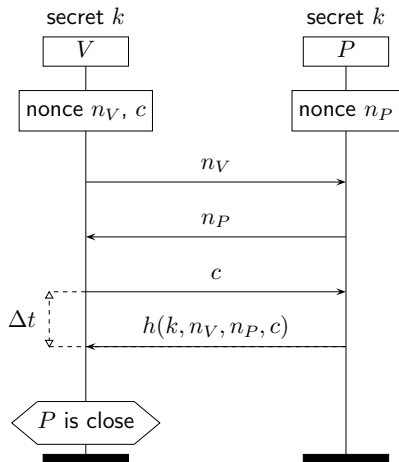
Example

Hancke and Kuhn's 2005



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$$\mathcal{P} = \{R_1, R_2, R_3, R_4, R_5\}$$

$$\frac{V \in Hnst \quad t \geq \text{max}(\alpha) \quad \text{fresh}(n_V, \alpha)}{(\alpha, (t, \text{send}_V(n_V))) \in R_1}$$

$$\frac{P \in Hnst \quad t \geq \text{max}(\alpha) \quad (t', \text{recv}_P(n_V)) \in \alpha \quad \text{fresh}(n_P, \alpha)}{(\alpha, (t, \text{send}_P(n_P))) \in R_2}$$

$$\frac{V \in Hnst \quad t \geq \text{max}(\alpha) \quad (t', \text{send}_V(n_V)) \in \alpha \quad (t'', \text{recv}_V(n_P)) \in \alpha \quad \text{fresh}(c, \alpha)}{(\alpha, (t, \text{send}_V(c))) \in R_3}$$

$$\frac{P \in Hnst \quad t \geq \text{max}(\alpha) \quad (t', \text{recv}_P(n_V)) \in \alpha \quad (t'', \text{send}_P(n_P)) \in \alpha \quad (t''', \text{recv}_P(c)) \in \alpha \quad r = h(\text{sh}(V, P), n_V, n_P, c)}{(\alpha, (t, \text{send}_P(r))) \in R_4}$$

$$\frac{V \in Hnst \quad t \geq \text{max}(\alpha) \quad (t', \text{send}_V(n_V)) \in \alpha \quad u = \text{send}_V(c) \quad (tu, u) \in \alpha \quad r = h(\text{sh}(V, P), n_V, n_P, c)}{(\alpha, (t, \text{claim}_V(P, u, v))) \in R_5}$$

- And some other stuff such as **message deduction**.

The set $\text{infer}(A, \alpha)$ contains all messages that A can infer from α :

$$\frac{m \in \text{init}(A)}{m \in \text{infer}(A, \alpha)} \quad \frac{(t, \text{recv}_A(m)) \in \alpha}{m \in \text{infer}(A, \alpha)} \quad \frac{(m_1, m_2) \in \text{infer}(A, \alpha)}{m_i \in \text{infer}(A, \alpha)}$$

$$\frac{m_1 \in \text{infer}(A, \alpha) \quad m_2 \in \text{infer}(A, \alpha)}{(m_1, m_2) \in \text{infer}(A, \alpha)} \quad \frac{m \in \text{infer}(A, \alpha) \quad f \in \text{Func} \setminus \{sk, {}^{-1}, sh\}}{f(m) \in \text{infer}(A, \alpha)}$$

$$\frac{m \in \text{infer}(A, \alpha) \quad k \in \text{infer}(A, \alpha)}{\{m\}_k \in \text{infer}(A, \alpha)} \quad \frac{\{m\}_k \in \text{infer}(A, \alpha) \quad k^{-1} \in \text{infer}(A, \alpha)}{m \in \text{infer}(A, \alpha)}$$

The set of all valid traces $Tr(\mathcal{P})$ is defined by:

$$\alpha \cdot (t, e) \in Tr(\mathcal{P}) \iff \\ \alpha \in Tr(\mathcal{P}) \wedge \exists R \in \mathcal{P} \cup \{Int, Net\}: (\alpha, (t, e)) \in R$$

where:

$$\frac{\begin{array}{l} I \in Dishonest \\ t \geq maxt(\alpha) \\ m \in infer(I, \alpha) \end{array}}{(\alpha, (t, send_I(m))) \in Int} \qquad \frac{\begin{array}{l} t \geq maxt(\alpha) \\ (t', send_A(m)) \in \alpha \\ t \geq t' + dist(A, B)/c \end{array}}{(\alpha, (t, recv_B(m))) \in Net}$$

Definition

A protocol \mathcal{P} satisfies *secure distance-bounding* if and only if:

$$\forall \alpha \in \text{Tr}(\mathcal{P}), (t, \text{claim}_V(P, u, v)) \in \alpha:$$

$$\exists (tu, u), (tv, v) \in \alpha, P' \approx P: \text{dist}(V, P') \leq \frac{c \cdot (tv - tu)}{2}$$

where $\approx = \{(A, A) \mid A \in \text{Honest}\} \cup \text{Dishonest} \times \text{Dishonest}$.

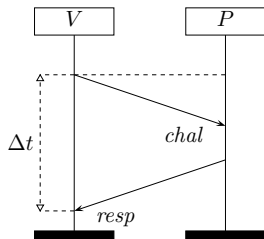
Implemented in Isabelle/HOL, available at

<http://www.infsec.ethz.ch/research/software/protoveriphy.html>

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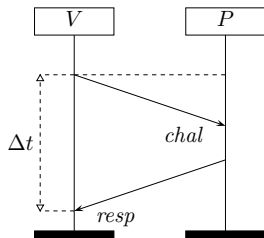
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Three timing scenarios

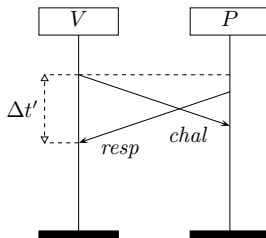


Correct timing

Three timing scenarios

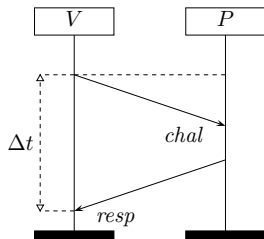


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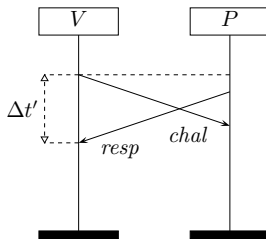


Early timing

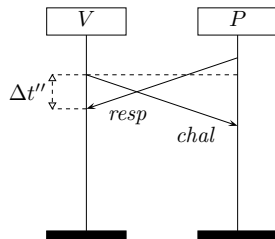
Three timing scenarios



Correct timing

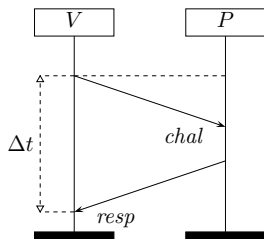


Early timing

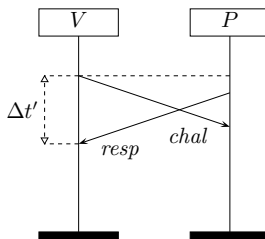


Very early timing

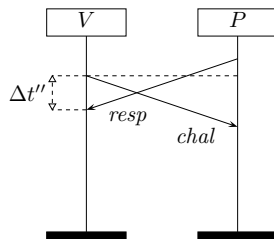
Three timing scenarios



Correct timing



Early timing



Very early timing

Claim: If there is an early timing, then there is a very early timing.

Theorem

A protocol \mathcal{P} satisfies secure distance-bounding if and only if:

$$\forall \sigma \in \pi(\text{Tr}(\mathcal{P})), \text{claim}_V(P, u, v) \in \sigma:$$

$$\exists u \cdot e \cdot v \sqsubseteq \sigma: \text{actor}(e) \approx P$$

where $\pi(T) = \{e_1 \cdots e_n \mid (t_1, e_1) \cdots (t_n, e_n) \in T\}$.

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Verified 12+ protocols in Tamarin, available at
<http://satoss.uni.lu/software/DBVerify/>

Towards the proof

April 5th, 2017

- 1 - time consistency
- 2 - speed of light consistency
- 3 - induction
- 4 - swap / independence
- 5 - returning
- 6 - permutation

1. $\forall x = (t, e) \dots (t_n, e_n) \quad i < j \Rightarrow t_i \leq t_j$
2. $\forall x = (t, e) \dots (t_n, e_n) \quad e \in \text{Recv} \quad \forall x \in T \text{ sol } \alpha$
 $\Rightarrow \exists (t', e') \in x \quad e' \text{ not } \wedge (t', e') \geq d(e, e')$
3. $\forall x = (t, e) \dots (t_n, e_n) \quad T(p) \Rightarrow x \in T(p)$
4. $\forall x = (t, e) \dots (t_n, e_n) \quad \left. \begin{array}{l} \alpha(t, e) \in T(p) \\ \alpha(t', e') \in T(p) \\ \alpha(t'', e'') \in T(p) \end{array} \right\} \Rightarrow \exists_{e'''} \alpha(t, e) \wedge \alpha(t', e') \wedge \alpha(t'', e'') \wedge \alpha(t''', e''') \in T(p)$
5. $\forall x, y = (t, e) \dots (t_n, e_n) \quad \forall e'' \quad \left. \begin{array}{l} \alpha(t, e) \wedge \alpha(t', e') \wedge \alpha(t'', e'') \wedge \alpha(t''', e''') \in T(p) \\ \wedge \alpha(t'', e'') \in T(p) \end{array} \right\} \Rightarrow \alpha(t, e) \wedge \alpha(t', e') \wedge \alpha(t'', e'') \wedge \alpha(t''', e''') \in T(p)$

$$\alpha(t, e) \wedge \alpha(t', e') \wedge \beta(t'', e'') \in T_r$$

$$\text{sol: } \alpha(x) \wedge \beta(x)$$

$$\alpha(t, e) \wedge \alpha(t', e') \wedge \beta(t'', e'') \in T_r$$

$$\alpha(t, e) \wedge \alpha(t', e') \wedge \alpha(t'', e'') \in T_r$$

$$\forall \alpha, \alpha' \in T_r \text{ s.t. } \alpha =_{Ev} \alpha' \quad \alpha(t, e) \Rightarrow \alpha'(t, e)$$

$$t_i = \max(t_i, e_i \mid e_i \in x)$$

$$\max(\max(t_i, e_i \mid e_i \in x), t_i + d(e, e'))$$

$$7. \forall (t_1, e_1) \dots (t_n, e_n) \in T_r \quad (t'_1, e'_1) \dots (t'_n, e'_n) \in T_r$$

$$\alpha(t, e) \in T_r \Rightarrow \alpha(t + d, e) \in T_r$$

$$e \in L \Leftrightarrow \exists t', t'' \in \mathbb{R} \quad \left. \begin{array}{l} \alpha(t', e) \in T_r \\ \alpha(t'', e) \in T_r \end{array} \right\} \quad \text{Def}$$

$$\left. \begin{array}{l} \alpha(t, e) \in T_r \\ \alpha(t', e') \in T_r \\ t \leq t' \end{array} \right\} \Rightarrow \alpha(t', e') \in T_r$$

$$\alpha(t, e) \in T_r \wedge \alpha(t', e') \in T_r \Rightarrow \alpha(t, e) \wedge \alpha(t', e') \in T_r$$

Proof idea

Characterise timed-traces model

For every $(t_1, e_1) \cdots (t_n, e_n) \in Tr(\mathcal{P})$:

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- ① $t_1 \leq \cdots \leq t_n$
- ② $t_n = \text{recv}_A(m)$ implies $i < n$ exists such that $e_i = \text{send}_B(m)$ and $t_n - t_i \geq \text{dist}(A, B) / c$

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- ③ if $(t'_1, e_1) \cdots (t'_n, e_n)$ satisfies (1) and (2) then $(t'_1, e_1) \cdots (t'_n, e_n) \in Tr(\mathcal{P})$

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For every $e_1 \cdots e_n \in \pi(Tr(\mathcal{P}))$:

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For every $e_1 \cdots e_n \in \pi(Tr(\mathcal{P}))$:

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For every $e_1 \cdots e_n \in \pi(Tr(\mathcal{P}))$:

- ① $e_1 \cdots e_{n-1} \in \pi(Tr(\mathcal{P}))$
- ② $e_n \notin Recv$ and $actor(e_{n-1}) \neq actor(e_n)$ then
 $e_1 \cdots e_{n-2} \cdot e_n \in \pi(Tr(\mathcal{P}))$

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 $e_1 \cdots e_{n-2} \cdot e_n \in \pi(Tr(\mathcal{P}))$
- ③ $e_n = send_A(m)$ implies $e_1 \cdots e_n \cdot recv_B(m) \in \pi(Tr(\mathcal{P}))$

Proof idea

Characterise timed-traces model

For every $e_1 \cdots e_n \in \pi(\text{Tr}(\mathcal{P}))$:

- ① $e_1 \cdots e_{n-1} \in \pi(\text{Tr}(\mathcal{P}))$
- ② $e_n \notin \text{Recv}$ and $\text{actor}(e_{n-1}) \neq \text{actor}(e_n)$ then $e_1 \cdots e_{n-2} \cdot e_n \in \pi(\text{Tr}(\mathcal{P}))$
- ③ $e_n = \text{send}_A(m)$ implies $e_1 \cdots e_n \cdot \text{recv}_B(m) \in \pi(\text{Tr}(\mathcal{P}))$
- ④ $\forall A, B \in \text{Honest}^2 \cup \text{Dishonest}^2$ it holds that $(e_1 \cdots e_n)[A \mapsto B] \in \pi(\text{Tr}(\mathcal{P}))$

The Tamarin dbsec lemma

```
lemma dbsec:
"
All P V m n #t. (
VerifierComplete(P, V, m, n)@t ) ==>
(
  Ex #tc.
    Corrupt(V)@tc
)| (
  Ex #t1 #t2 #t3.
    StartFastPhase(V, m)@t1 &
    Action(P)@t2 &
    EndFastPhase(V, m)@t3 &
    (#t1 < #t2) &
    (#t2 < #t3) &
    ( (#t3 < #t ) | (#t3 = #t) )
)| (
  Ex CAgent #t4 #t5 #t6 #t7.
    StartFastPhase(V, m)@t5 &
    EndFastPhase(V, m)@t7 &
    Corrupted(P, V)@t4 &
    CAction(CAgent)@t6 &
    (#t5 < #t6)&
    (#t6 < #t7)&
    ( (#t7 < #t) | (#t7 = #t) )
)
"
```

Verification in Tamarin

Protocol	Satisfies dbsec?	Attack found
BC-Signature	No	DH
BC-FiatShamir	No	DH, DF
BC-Schnorr	No	DH, DF
CRCS	No	DH
Meadows et al.	No	DH
Tree-based	Yes	-
Poulidor	Yes	-
Hancke and Kuhn	Yes	-
Uniform	Yes	-
Kim and Avoine	Yes	-
Munilla et al.	Yes	-
Reid et al.	Yes	-
Swiss-Knife	Yes	-
TREAD-PK	No	MF, DH
TREAD-SH	No	DH
PaySafe	No	DF, DH

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What we achieved

- Proved that secure distance-bounding can be formulated through causality.
- Provided a fully-automatic verification framework for DB protocols. (simply specify the protocol and click on “verify dbsec lemma”).
- Provided computer-verifiable (in)security proofs for a number of state-of-the-art protocols.
- Identified *unreported* vulnerabilities in two published protocols: PaySafe (FC’15) and TREAD (AsiaCCS’17).

Outline

- 1 Introduction
- 2 Probabilistic model based on automata
- 3 Symbolic model with time and location
- 4 Symbolic model based on causality
- 5 Conclusion and Future

Probabilistic vs. Symbolic

- Where probabilistic models win:
 - More precise results - there's an attack that succeeds w/ prob. p
 - Arithmetic properties can be fairly-well modeled
- Where symbolic models win:
 - No need to consider each attack individually
 - Automated verification - Tamarin, ProVerif, Scyther, Isabelle
 - Computer-verifiable proofs of (in)security

- Terrorist fraud?
Requires fancy techniques for corruption modeling.

- Terrorist fraud?
Requires fancy techniques for corruption modeling.
- Automatic probabilistic analysis?
Seems hard.

Thank you

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